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EXTREME MEAN AND ITS APPLICATIONS

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and

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#### EXTREME MEAN AND ITS APPLICATION

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### INTRODUCTION

In applications where observations are assumed to follow a normal distribution, very often interest centers around the extreme value, since in some sense, such a value indicates the tolerance of a system. The maximum or minimum sample values in such applications are of limited usefulness, because maximum and minimum tend to extend with increasing sample sizes. Moreover, the information actually sought may not pertain to the actual extreme values, but rather may be needed for the values falling above or below some preassigned p-th percentile. In a given application (ref. 1) the information may be needed on the values falling above the 99th percentile. For such an application, the method of extreme mean is presented in this study.

The extreme mean in this study is defined as the mean of a truncated normal distribution above or below a preassigned p-th percentile. An unbiased estimate of this extreme mean is obtained and its variance is then compared with the Cramer-Rao lower bound. Further, the distribution of the standard-ized estimate and various confidence intervals are obtained.

The distortion parameters data obtained from high frequency response pressure measurements made at the inlet/engine interface plane during a YF-12 flight experiment (ref. 1) are used to demonstrate the usefulness of extreme mean in applications.

### **SYMBOLS**

```
Α
                   = (1\sqrt{n}) + af/\sqrt{2(n-1)}
                   Constants corresponding to extreme mean and variance
a,b
                   = f\sqrt{(2n-3)/(2n-2)} - 1
В
                   = \sqrt{(1 + d)/2n(n - 1)}
C
                   Solution to equation \Phi[(c_p - \mu)/\sigma] = p
                   = \sqrt{2n - 3}
D
D(T)
                   Density function of T
                   = na^2 (f^2 - 1)
d
Ε
                   Expectation of random variable
F(T)
                   Distribution function of T
                   = \sqrt{(n-1)/2} \Gamma[(n-1)/2]/\Gamma(n/2)
f
f(x)
                   Density function of the truncated normal distribution
I<sub>11</sub>, I<sub>12</sub>, I<sub>22</sub>
                   Elements of information matrix
IDT
                   Measure of simple distortion
i
                   Sample number
K_{\Delta}
                   Measure of combined circumferential and radial distortion
Kr
                   Measure of radial distortion
K
                   Measure of circumferential distortion
L,U
                   Lower and upper confidence bounds
1,u
                   Lower and upper confidence bounds of standardized distribution
                   Length of confidence interval
2m
                   Sample size
n
                   Probability of event
                   Percentile assigned for extreme mean
                   Sample standard deviation
```

=  $(\hat{\mu}_E - \mu_E) / \hat{\sigma}_{\mu_E}$ , standardized extreme mean variable Τ Sample values  $X_1, \dots, X_n$ x Sample mean Chi Square random variable with r degrees of freedom Z Standard normal random variable Confidence level α, ALPHA  $\Gamma(x)$ Gamma function Mean of normal distribution u, MU Extreme mean  $\mu_{\mathsf{F}}$ Standard deviation of normal distribution o, SIGMA

Estimate of associated  $\mu$  or  $\sigma$ 

Standard normal distribution function

σE

^, HAT

 $\Phi(x)$ 

FORMULAE FOR EXTREME MEAN  $\boldsymbol{\mu}_{\boldsymbol{F}}$  AND ITS UNBIASED ESTIMATE

Standard deviation of truncated normal distribution

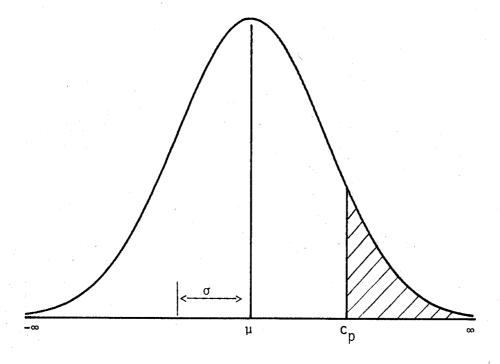
Let  $x_1$ ,  $x_2$ ,...,  $x_n$  be a random sample of size  $\,n\,$  from a normal distribution with unknown population parameters, mean  $\,\mu\,$  and standard deviation  $\,\sigma\,$ , shown in figure 1. The extreme mean  $\,\mu_E\,$  is defined as the mean of the truncated distribution shown in figure 1, truncated at  $\,c_p\,$  depending on the preassigned value of  $\,p\,$ . The sample provides a sample mean,  $\,\bar{x}\,$ , and a sample standard deviation,  $\,p\,$ , which are sufficient statistics (ref. 2) to estimate any function of  $\,\mu\,$  and  $\,p\,$ . These statistics are independent and are employed in the estimation of  $\,\mu\,$  and its distribution.

Truncated Distribution Mean  $\mu_E$  and Variance  $\sigma_E^{\ 2}$ 

The density function of a truncated normal distribution is

$$f(x) = [(1 - p)\sigma\sqrt{2\pi}]^{-1} \exp\{-[(x - \mu)/\sigma]^2/2\}; x > c_p$$

where p =  $\Phi$  (c<sub>p</sub> -  $\mu$ )/ $\sigma$  is preassigned and represented by the unshaded portion of the normal distribution in figure 1. For a given  $\mu$  and  $\sigma$ , c<sub>p</sub> can be obtained from standard normal tables. From the density function, the expres-



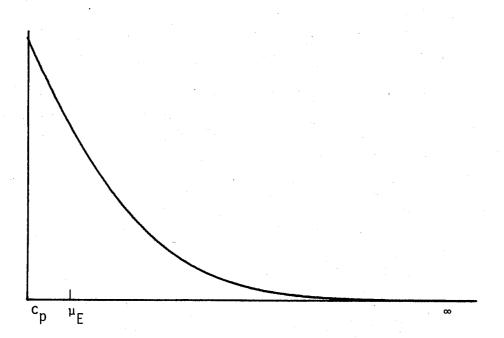


Figure 1. Normal distribution with mean  $\mu$  and standard deviation  $\sigma$  , and truncated normal distribution truncated at  $c_p$  corresponding to p-th percentile.

sions for  $\mu_E$  and  $\sigma_E^{\ 2}$  are

$$\mu_{E} = [(1 - p)\sigma \sqrt{2\pi}]^{-1} \int_{C_{p}}^{\infty} x \exp \{-[(x - \mu)/\sigma]^{2}/2\} dx$$

$$= \mu + a\sigma$$

$$\sigma_{E}^{2} = [(1 - p)\sigma \sqrt{2\pi}]^{-1} \int_{C_{p}}^{\infty} x^{2} \exp \{-[(x - \mu)/\sigma]^{2}/2\} dx - \mu_{E}^{2}$$

$$= b\sigma^{2}$$

where

$$a = [(1 - p) \sqrt{2\pi}]^{-1} \exp \{-[(c_p - \mu)/\sigma]^2/2\}$$

$$b = [(1 - p) \sqrt{2\pi}]^{-1} \left( \sqrt{2} \left\{ r(3/2) - \int_{0}^{(c_p - \mu)/\sigma} \frac{^{2}}{^{2}} [exp(-t)] t^{1/2} dt \right\} - a \right)$$

For any specific value of p, the values of a and b can be obtained with the available tables of complete and incomplete Gamma functions. For example, for p = .90,  $c_p = 1.282$ , the corresponding value of a = 1.7541 and b =  $(.395)^2$ .

Unbiased Estimate of  $\boldsymbol{\mu}_{\text{F}}$ 

It is to be noted that

$$\bar{x} = (\Sigma x_i)/n$$

and

$$s = [\Sigma(x_i - x)^2/(n - 1)]^{\frac{1}{2}}$$

are sufficient statistics from the sample, and must be employed in the estimation of  $\mu_{\mbox{\scriptsize F}}.$  Further

$$E(\bar{x}) = \mu$$
;  $E(s) = \sigma \sqrt{2/(n-1)} \Gamma(n/2) / \Gamma(n-1)/2$ 

and

$$Var(\bar{x}) = \sigma^2/n$$
;  $Var(s) = \sigma^2 \left(1 - \left(\sqrt{2}r(n/2)\right) / \sqrt{(n-1)} r[(n-1)/2]\right)^2$ 

Thus an unbiased estimate of  $\mu_{\text{F}}$  is given by

$$\hat{\mu}_{E} = \bar{x} + as \sqrt{(n-1)/2} r [(n-1)/2] / r(n/2)$$

$$= \bar{x} + asf$$

where a was derived in the section on truncated distributions, and

$$f = \sqrt{(n-1)/2} \Gamma [(n-1)/2] / \Gamma (n/2)$$

depends on the sample size n via Gamma function values.

Since  $\bar{x}$  and  $s^2$  are stochastically independent, the variance of the unbiased estimate  $\mu_F$  is

$$Var(\hat{\mu}_{E}) = Var(\bar{x}) + a^{2}f^{2}Var(s)$$

$$= \sigma^{2}/n + a^{2}f^{2}Var(s)$$

$$= \sigma^{2}/n + a^{2}f^{2}\sigma^{2}(1 - f^{-2})$$

$$= (\sigma^{2}/n) \left[1 - na^{2}(f^{2} - 1)\right]$$

$$= \hat{\sigma}_{\mu_{E}}^{2}$$

In this expression, sample size n, a and f are known; and the only unknown factor is  $\sigma^2$ . Thus an estimate of  $\text{Var}(\hat{\mu}_E)$  can be obtained by replacing  $\sigma^2$  by  $s^2$  obtained from the sample. Therefore,

$$Var(\hat{\mu}_{E}) = (s^{2}/n) [1 + na^{2}(f^{2} - 1)]$$
$$= (s^{2}/n)(1 + d)$$
$$= \hat{\sigma}_{\mu_{E}}^{2}$$

This estimate is different from  $s^2/n$  by a factor of  $d=na^2(f^2-1)$ , which is a function of n; and even for sufficiently large n, the factor d is not negligible.

# Cramer-Rao Lower Bound of Variance of $\hat{\mu}_{\text{F}}$

Variance of the estimate  $\hat{\mu}_E$  measures, in some sense, the quality of the unbiased estimate. The smaller the variance, the better the estimate. An unbiased estimate is considered best if it achieves the minimum possible variance without specifying the estimate. The Cramer-Rao lower bound for  $\bar{x}$  and s are

$$Var(\bar{x}) \ge 1/E$$
  $\frac{\partial}{\partial \mu} \ln f(\bar{x},s)^2 = 1/I_{11}$   
 $Var(s) \ge 1/E$   $\frac{\partial}{\partial \sigma} \ln f(\bar{x},s)^2 = 1/I_{22}$ 

In many cases, it is possible to find an unbiased estimate which achieves this bound. In other cases, it is never attainable. In this section, the lowest bound is obtained and then compared with the variance  $\hat{\mu}_E$  computed in the earlier section.

The joint distribution of  $\bar{x}$  and s is (ref. 3)

$$f(\bar{x},s) = k_n(s^{(n-2)}/\sigma^n) \exp \left\{ -[(\bar{x} - \mu) \sqrt{n}/\sigma]^2 - (n-1)s^2/\sigma^2 \right\} / 2$$

where

$$kn = \left[2\sqrt{n} (n-1)^{(n-1)/2}\right] / \left\{\sqrt{2\pi} 2^{(n-1)/2} r [(n-1)/2]\right\}$$

Thus

$$\ln f(\bar{x},s) = \ln k_n + (n-2)\ln s - n \ln \sigma - \left\{ \left[ (\bar{x} - \mu)\sqrt{n}/\sigma \right]^2 + (n-1)s^2/\sigma^2 \right\} / 2$$

where  $k_n$  is the first factor in  $f(\bar{x},s)$ . From the expression for  $\ln f(\bar{x},s)$ , it is seen by differentiating that

$$\frac{\partial}{\partial \mu} \ln f(\bar{x},s) = \left[ (\bar{x} - \mu) \sqrt{n} / \sigma \right] (\sqrt{n} / \sigma)$$

$$\frac{\partial}{\partial \sigma} \ln f(\bar{x},s) = -(n/\sigma) + \left[ (\bar{x} - \mu) \sqrt{n} \right]^2 + \left[ (n-1)s^2 \right] \left[ 2/\sigma^3 \right]$$

$$= (1/\sigma) \left[ (\bar{x} - \mu) \sqrt{n} / \sigma \right]^2 + (n-1)s^2 / \sigma^2 - n$$

The Cramer-Rao lower bound for  $\bar{x}$  and s from these expressions is already given.

It is known that the distribution of  $\left[(\bar{x}-\mu)\sqrt{n}/\sigma\right]^2$  is Chi Square with 1 degree of freedom. The distribution of (n-1) s $^2/\sigma^2$  is Chi Square with (n-1) degrees of freedom. The two distributions are independent. If  $Y_r$  is a Chi Square variable with r degrees of freedom, then  $E(Y_r)=r$  and  $E(Y_r^2)=2r+r^2$ . Therefore

$$\begin{split} I_{11} &= (n/\sigma^2) \ E \left[ (\bar{x} - \mu) \sqrt{n} / \sigma \right]^2 \\ &= n/\sigma^2 \\ I_{22} &= (1/\sigma^2) \ E \quad Y_1 + Y_{(n-1)} - n^2 \\ &= (1/\sigma^2) \ E \quad Y_1^2 + Y_{(n-1)}^2 + n^2 + 2Y_1 Y_{(n-1)} - 2n Y_1 + Y_{(n-1)} \\ &= (1/\sigma^2) \left\{ (2+1) + \left[ 2(n-1) + (n-1)^2 \right] + n^2 + 2(n-1) - 2n^2 \right\} \\ &= 2n/\sigma^2 \end{split}$$

Thus the lowest bound of the variance of  $\hat{\mu}_E = \bar{x} + afs$  is obtained by the appropriate function of inverses of  $I_{11}$  and  $I_{22}$ . Therefore

Var 
$$\hat{\mu}_{E} \ge 1/I_{11} + a^{2}f^{2}/I_{22}$$
  
 $\ge \sigma^{2}/n + a^{2}f^{2}\sigma^{2}/2n$ 

The expression for the variance of  $\hat{\mu}_{E}$  obtained in the earlier section is

$$Var \hat{\mu}_E = \sigma^2/n + a^2\sigma^2(f^2 - 1)$$

which is larger than the lower bound shown above by a factor of  $a^2\sigma^2\left[(f^2-1)-f^2/2n\right]$ . For larger values of n, this factor's value decreases;

therefore,  $\hat{\mu}_E$  is a satisfactory estimate of  $\mu_E$  for all applications. In fact, as n approaches infinity, the variance of the estimate achieves the Cramer-Rao lower bound.

Large Sample Distribution of T = 
$$(\hat{\mu}_E - \mu_E) / \hat{\sigma}_{\mu_E}$$

The exact distribution of  $\hat{\mu}_E = \bar{x} + afs$  depends on the sum of both the normal and Chi Square distributions. However, for a large sample (n > 30), an approximate distribution is available which can be used to compute confidence bounds.

It is to be noted that the distribution of  $(\bar{x} - \mu)\sqrt{n}/\sigma = Z$  is standard normal, that the distribution of  $(n-1)s^2/\sigma^2$  is Chi Square with (n-1) degrees of freedom, and these distributions are independent of one another. For a large sample  $(n \ge 30)$ , the distribution can be approximated by

$$Z = \sqrt{2Y_{(n-1)}} - \sqrt{2(n-1)} - 1$$
$$= (s/\sigma) \sqrt{2(n-1)} - \sqrt{2n-3}$$

which yields

$$s/\sigma = \left[\sqrt{2(n-1)}\right]^{-1} \left(Z + \sqrt{2n-3}\right)$$

In this section, instead of finding the distribution of  $\hat{\mu}_E$ , the distribution of the standardized T =  $(\hat{\mu}_E - \mu_E)/\hat{\sigma}_{\mu_E}$  is obtained by the above approximation of s/ $\sigma$ .

$$T = (\hat{\mu}_{E} - \mu_{E})/\hat{\sigma}_{\mu_{E}}$$

$$= \left[ (\bar{x} + afs) - (\mu + a\sigma) \right] / s\sqrt{(1 + d)/n}$$

$$= \left\{ (1/\sqrt{n}) \left[ (x - \mu)\sqrt{n}/\sigma \right] \sigma + a\sigma(fs/\sigma - 1) \right\} \left[ \sigma(s/\sigma)\sqrt{(1 + d)/n} \right]^{-1}$$

$$\simeq \frac{(Z/\sqrt{n}) + a\sigma}{\sqrt{(1 + d)/n} \left[ (Z + \sqrt{2n - 3}) / \sqrt{2(n - 1)} \right] - 1}$$

$$\simeq \frac{Z \left[ (1/\sqrt{n}) + af/\sqrt{2(n - 1)} \right] + a \left[ f\sqrt{(2n - 3)/(2n - 2)} - 1 \right]}{\sqrt{(1 + d)/2n(n - 1)} \left( Z + \sqrt{2n - 3} \right)}$$

$$\simeq (ZA + B)/C(Z + D)$$

where

A = 
$$(Z/\sqrt{n}) + af/\sqrt{2(n-1)}$$
  
B =  $a(f\sqrt{(2n-3)/(2n-2)} - 1)$   
C =  $\sqrt{(1+d)/2n(n-1)}$   
D =  $\sqrt{2n-3}$ 

are functions of the sample size n and a preassigned value of p. Since Z has a standard normal density, the density function of T is given by

$$D(t) = [C(AD - B)/\sqrt{2\pi}](A - Ct)^{-2} exp \{-[(CDt - B)/(A - Ct)]^{2}/2\}$$

This density function does not depend on  $\mu$  or  $\sigma,$  but is a function of the sample size n and the preassigned value of p. Appendix B lists the computer program which generates the density and distribution function of T for a designated sample size n and value of p. A sample of the density of T for n = 90 and p = .90 is tabulated in Table 1 and shown in figure 2. Figure 2 also contrasts the density of T with a standard normal density.

# Confidence Intervals of $\mu_{\mbox{\footnotesize E}}$

A confidence interval is either specified by assigning a level of confidence  $\alpha,$  or by assigning the length of the confidence interval 2m. In the first case, lower and upper confidence bounds L and U are obtained which, in a long series of experiments, are likely to include the population  $\mu_E$ ,  $\alpha\%$  of times. In the second case, the values of L and U are fixed and the level  $\alpha$  is obtained. Analytically both the cases involve solving for either L, U or  $\alpha$ , given the other.

Confidence interval with  $\alpha$  confidence. - In this case, the equation

$$Pr [1 < (ZA + B)/C(Z + D) < u] = \alpha$$

needs to be solved. Since Z is a standard normal variate, it follows that

$$1 = \left(-Z_{\alpha/2}A + B\right) / \left[C(-Z_{\alpha/2}) + D\right]$$

$$u = \left(Z_{\alpha/2}A + B\right) / \left(CZ_{\alpha/2} + D\right)$$

where Z  $_{\alpha/2}$  is obtained from a normal probability table. For these expressions, it is seen that the lower and upper confidence values, L and U, for  $\mu_E$  are

$$L = \bar{x} + afs - us \sqrt{(1 + d)/n}$$

$$U = \bar{x} + afs + 1s \sqrt{(1 + d)/n}$$

TABLE 1. DENSITY ( D(T) ) AND DISTRIBUTION ( F(T) ) OF THE RANDOM VARIABLE T = (MU HAT - MU)/S(MU HAT) N = 90

T	D(T)	F(T)	T	O(T)	F(T)
-5.00	.003591	.002637	0.00	.281669	.500024
		.003020		.283965	528317
-4.90	.004093		•10		
-4.80	.004662	.003457	.20	.284827	•556769
-4.70	• 0 0 530 4	.003955	•30	.284193	•585232
-4.60	.006029	.004521	. 40	.282027	•613556
-4.50	.006846	.005164	•50	.278312	.641586
-4.40	.007766	.005894	.60	.273062	.669168
				.266315	.696149
-4.30	.008799	.00€721	•70		
-4.20	.009958	.007658	.80	.258136	.722383
-4.10	.011257	.008717	• 90	.248620	•747731
	0.4.27.0.0	0.00047	1.00	.237884	.772066
-4.00	.012709	.009914			
-3.90	.014329	.011265	1.10	.226069	. 795272
-3.80	.01€135	.0127.66	1.20	•213339	.817249
-3.70	.018143	.014498	1.30	•199872	.837915
-3.60	.020371	.016422	1.40	•185859	.857206
-3.50	.022840	.018581	1.50	.171496	.875075
-3.40	025557	.020999	1.60	.156985	.891500
					.906474
-3.30	.028575	• 023703	1.70	•142521	
-3.20	.031884	.026724	1.80	.128292	.920012
-3.10	.035515	.030091	1.90	•114471	.932146
-3.00	.039489	.033838	2.00	.101214	.942925
		.03 8001	2.10	.088656	.952412
-2.90	.043827			.076905	
-2.80	.048549	.042616	2.20		.960683
-2.70	.053673	.047724	2.30	• 0 66046	• 967823
-2.60	.059218	.053365	2.40	.056136	. 97 3924
-2.50	.065199	.05 (582	2.50	.0 47204	.979083
-2:40	.071626	. 166420	2.60	.039256	.983398
-2.30	.078510	.073923	2.70	.0 32275	. 986966
-2.20	.085856	.082137	2.80	.026223	. 989883
					992240
-2.10	.093662	.091109	2.90	021047	4 776640
-2.00	.101924	.100 885	3,00	.016680	.994120
-1.90	.110628	.111509	3.10	.013048	.995600
-1.80	.119757	.123024	3.20	.010070	996751
				.00766.3	.997633
-1.70	.129283	.135473	3.30	_	
-1.60	.139170	.148893	3.40	.005748	.998300
-1.50	• 1 49374	.163318	3.50	.0 (4248	• 998797
-1.40	•159839	.178777	3.60	.0C3091	• 999161
-1.30	.170502	.195292	3.70	.002213	.999424
-1.20	.181287	.212881	3.80	.001559	.999611
-1.10	.192110	.231551	3.90	.001079	.999742
-1010	•192110	• 201331		***************************************	• > > > • • •
-1.00	.202877	.251301	4.00	.000734	•999832
90	.213482	.272121	4.10	.000498	. 999892
80	. 223815	293989	4.20	.000321	•999932
70	• 233755	.316871	4.30	.000206	999958
		.340722	4.48	.000130	999975
60	.243178				
<b></b> 50	. 251954	. 365485	4.50	.000080	.999985
40	•259953	.391087	4.60	.000048	• 999991
30	.267046	• 417445	4.70	.0(0028	• 999995
20	.273107	. 444462	4.80	.000016	. 999997
10	.278018	.472028	4.90	.000009	• 999999
-					

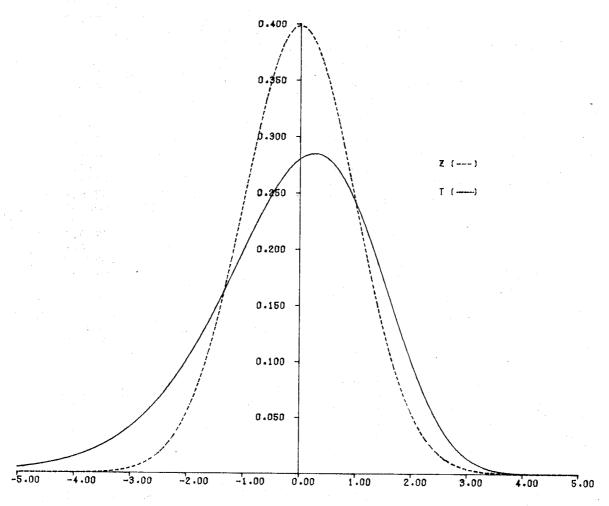


Figure 2. Density function of the standard normal variate Z, and the density function of the standardized extreme mean variate T.

Confidence interval of fixed length 2m.- In this case, it is already known that  $L = \mu_E - m$  and  $U = \mu_E + m$ . The object, therefore, is to find the corresponding value of  $\alpha_m$ . Since  $\sigma_{\mu_E} = s\sqrt{(1+d)/n}$  in the terms of standardized T variable, it is required to find

$$\alpha_{\text{m}} = \Pr \left[ -m/s\sqrt{(1+d)/n} < T < m/s\sqrt{(1+d)/n} \right]$$

$$\alpha_{\text{m}} = \Pr \left[ -m/s\sqrt{(1+d)/n} < (ZA + B)/C(Z + D) < m/s\sqrt{(1+d)/n} \right]$$

$$= \Pr \left[ Z_{L} < Z < Z_{U} \right]$$

$$= \Phi(Z_{U}) - \Phi(Z_{L})$$

The right-hand side can be read from standard normal probability tables after calculating  $Z_{i}$  and  $Z_{i}$  which are given below.

$$Z_{L} = mCD/s\sqrt{(1 + d)/n} + B / A + mC/s\sqrt{(1 + d)/n}$$
  
 $Z_{U} = mCD/s\sqrt{(1 + d)/n} - B / A - mC/s\sqrt{(1 + d)/n}$ 

A table of confidence bounds for standardized T for various sample sizes are given in Appendix A for ready use.

#### APPLICATION TO FLIGHT DATA

To demonstrate the usefulness of extreme mean estimation, data are obtained on distortion parameter IDT,  ${\rm K}_{\rm A},~{\rm K}_{\rm O},$  and  ${\rm K}_{\rm r}$  from high frequency response pressure measurements made at the inlet/engine interface plane during a supersonic aircraft propulsion research program (ref. 1). The summarized data are presented in Table 2. The data show the sample size, the sample mean  $(\bar{\rm x})$  and standard deviation  $(\vartheta)$  for all distortion parameters.

The succeeding four tables, numbered 3, 4, 5, and 6, show the extreme means and their lower and upper 95% confidence bounds for  $\alpha$  = .95 . Tables 7, 8, 9, and 10 present corresponding values for  $\alpha$  = .99 .

TABLE 2. SUMMARY OF DISTORTION PARAMETERS' DATA

SAMPLE #	SAMPLE SIZE	x	IDT ∂	×κΑ	ô	χ̈́	θ δ	x Kr	^
π	SIZL	-^	0		<u> </u>	×	<u> </u>	X	ô .
1	470	.137	.012	.875	.084	.377	.068	.498	.049
2	470	.167	.013	1.285	.119	.767	.101	.518	.067
3	470	.194	.017	1.050	.082	.400	.065	.650	.050
4	470	.207	.016	1.088	.081	.360	.074	.729	.056
5	470	.225	.018	1.170	.095	.443	.076	.727	.062
6	406	.118	.012	.744	.071	.414	.060	.330	.038
7	406	.120	.014	.572	.052	.297	.043	.275	.029
8	406	.186	.032	.886	.149	.519	.128	.367	.106
9	406	.177	.015	.834	.079	.264	.059	.570	.043
10	406	.200	.019	.891	.109	.373	.074	.518	.057
						-			
11	448	.194	.012	1.075	.093	.377	.078	.697	.055
12	448	.226	.013	1.153	.103	.415	.090	.738	.057
13	448	.257	.027	1.514	.136	.541	.112	.973	.093
14	448	.184	.014	.682	.058	.302	.047	. 381	.036
15	448	.206	.015	.731	.074	.314	.059	.418	.043
				•		·			

TABLE 3. 95 PERCENT CONFIDENCE INTERVALS FOR EXTREME MEAN, MU + 2.06 SIGMA (DATA: IDT)

SAMPLE NUMBER	SAMPLE SIZE	SAMPLE MEAN	SAMPLE STD DEV	LOWER	UPPER BOUND
1	470	.1370	.0120	. 1596	. 1641
2	470	. 1670	.0130	. 1915	. 1964
3	470	. 1940	.0170	.2261	.2324
4	470	.2070	.0160	.2372	.2432
5 6	470	.2250	.0180	.2590	.2657
6	406	.1180	.0120	. 1405	.1453
7	406	.1200	.0140	.1462	. 1519
8	406	.1860	.0320	.2460	. 2589
9	406	.1770	.0150	.2051	.2112
10	406	.2000	.0190	.2356	. 2433
11	448	. 1940	.0120	.2166	.2212
12	448	.2260	.0130	.2505	.2555
13	448	.2570	.0270	.3073	.3182
14	448	.1840	.0140	.2104	.2157
15	448	.2060	.0150	.2342	.2400

TABLE 4. 95 PERCENT CONFIDENCE INTERVALS FOR EXTREME MEAN, MU + 2.06 SIGMA (DATA: KA)

SAMPLE	SAMPLE	SAMPLE	SAMPLE	LOWER	UPPER
NUMBER	SIZE	MEAN	STD DEV	BOUND	BOUND
1	470	.8750	.0840	1.0335	1.0649
2	470	1.2850	.1190	1.5095	1.5541
3	470	1.0500	.0820	1.2047	1.2354
3 4	470	1.0880	.0810	1.2408	1.2712
5	470	1.1700	.0950	1.3492	1.3848
6	406	.7440	.0710	.8770	.9057
7 8	406	.5720	.0520	.6694	.6904
8	406	.8860	.1490	1.1652	1.2253
9	406	.8340	.0790	.9820	1.0139
10	406	.8910	.1090	1.0953	1.1392
11	448	1.0750	.0930	1.2501	1.2858
12	448	1.1530	.1030	1.3469	. 1.3864
13	448	1.5140	.1360	1.7700	1.8222
14	448	.6820	.0580	.7912	.8134
15	448	.7310	.0740	.8703	.8987

TABLE 5. 95 PERCENT CONFIDENCE INTERVALS FOR EXTREME MEAN, MU + 2.06 SIGMA (DATA: K<sub>Q</sub>)

	•				
SAMPLE NUMBER	SAMPLE SIZE	SAMPLE MEAN	SAMPLE STD DEV	LOWER BOUND	UPPER BOUND
	li er o				
	470	.3770	.0680	.5053	.5308
2	470	.7670	.1010	.9575	.9954
3	470	.4000	.0650	.5226	.5470
4	470	.3600	.0750	.5015	.5296
5	470	.4430	.0760	.5864	.6149
6	406	.4140	.0600	.5264	.5506
7	406	.2970	.0430	.3776	.3949
8	406	.5190	.1280	.7589	.8105
9	406	.2640	.0590	.3746	.3984
10	406	.3730	.0740	.5117	.5415
11	448	.3770	.0780	.5238	.5538
12	448	.4150	.0900	.5844	.6190
13	448	.5410	.1120	.7518	.7948
14	448	.3020	.0470	.3905	4085
15	448	.3140	.0590	.4251	.4477

TABLE 6. 95 PERCENT CONFIDENCE INTERVALS FOR EXTREME MEAN, MU + 2.06 SIGMA (DATA: K<sub>R</sub>)

SAMPLE	SAMPLE	SAMPLE	SAMPLE	LOWER	UPPER
NUMBER	SIZE	MEAN	STD DEV	BOUND	BOUND
1	470	.4980	.0490	.5904	.6088
2	470	.5180	.0670	.6444	.6695
3	470	.6500	.0500	.7443	.7631
. 4	470	.7290	The state of the s		
			.0560	.8346	.8556
5	470	.7270	.0620	.8440	.8672
6	406	.3300	.0380	.4012	.4165
7	406	.2750	.0290	.3293	.3410
δ	406	.3670	.1060	.5656	.6084
9	406	.5700	.0430	.6506	.6679
10	406	.5180	.0570	.6248	.6478
11	448	.6970	.0550	.8005	.8217
12	448	.7380	.0570	.8453	.8672
13	448	.9730	.0930	1.1481	1.1838
14	448	.3810	.0360	. 448'8	.4626
15	448	.4180	.0430	.4989	.5155
			• • • • •	. 7707	• ) • )

TABLE 7. 95 PERCENT CONFIDENCE INTERVALS FOR EXTREME MEAN, MU + 2.67 SIGMA (DATA: IDT)

SAMPLE	SAMPLE	SAMPLE	SAMPLE	LOWER	UPPER
NUMBER	SIZE	MEAN	STD DEV	BOUND	BOUND
. 1	470	.1370	.0120	.1655	.1730
2	470	.1670	.0130	.1979	.2060
3	470	. 1940	.0170	.2344	.2450
4	470	.2070	.0160	. 2451	.2550
5	470	.2250	.0180	.2673	.2790
ő	406	.1180	.0120	.1463	. 1544
7	406	.1200	.0140	.1530	.1624
	406	.1000	.0320	. 2615	.2830
8 9	406	.1770	.0150	.2124	.2225
10	406	.2000	.0190	. 2448	.2576
11	448	.1940	.0120	.2225	.2301
12	448	.2260	.0130	.2568	. 2651
13	448	.2570	.0270	.3210	.3383
14	448	. 1840	.0140	.2172	.2262
15	448	.2060	.0150	.2416	.2512

TABLE 8. 95 PERCENT CONFIDENCE INTERVALS FOR EXTREME MEAN, MU + 2.67 SIGMA (DATA: K<sub>A</sub>)

SAMPLE	SAMPLE	SAMPLE	SAMPLE	LOWER	UPPER
NUMBER	SIZE	MEAN	STD DEV	BOUND	BOUND
. 1	470	.8750	.0840	1.0748	1.1272
2	470	1,2850	.1190	1.5680	1.6423
3	470	1.0500	.0820	1.2450	1.2962
. 4	470	1.0880	.0810	1.2807	1.3312
5	470	1.1700	.0950	1.3960	1.4552
6	406	.7440	.0710	.9114	.9591
· 7	406	.5720	.0520	.6946	.7296
8	406	. 8860	.1490	1.2374	1.3375
9	406	.8340	.0790	1.0203	1.0734
10	406	.8910	.1090	1.1481	1.2213
11	448	1.0750	.0930	1.2956	1.3550
12	448	1.1530	.1030	1.3973	1.4631
13	448	1.5140	.1360	1.8366	1.9235
1.4	448	.6820	.0580	.8196	.8566
15	448	.7310	.0740	.9065	.9538

TABLE 9. 95 PERCENT CONFIDENCE INTERVALS FOR EXTREME MEAN, MU + 2.67 SIGMA (DATA:  $K_{\Theta}$ )

SAMPLE	SAMPLE	SAMPLE	SAMPLE	LOWER	UPPER
NUMBER	SIZE	MEAN	STD DEV	BOUND	BOUND
1	470	.3770	.0680	.5387	.5811
2	470	.7670	.1010	1.0072	1.0702
3	470	.4000	.0650	.5546	5951
4	470	.3600	.0750	.5384	.5852
5	470	.4430	.0760	.6238	.6712
6	406	.4140	.0600	.5555	.5852
7	406	.2970	.0430	.3984	.4273
8	406	.5190	.1280	.8209	.9069
9	406	.2640	.0590	.4031	.4428
10	406	.3730	.0740	.5475	.5972
11	448	.3770	.0780	.5620	.6119
12	448	.4150	.0900	.6285	.6860
13	448	.5410	.1120	.8067	.8782
14	448	.3020	.0470	.4135	4435
15	448	.3140	.0590	.4540	.4917

TABLE 10. 95 PERCENT CONFIDENCE INTERVALS FOR EXTREME MEAN, MU + 2.67 SIGMA (DATA: K<sub>R</sub>)

	;				
SAMPLE	SAMPLE	SAMPLE	SAMPLE	LOWER	UPPER
NUMBER	SIZE	MEAN	STD DEV	BOUND	BOUND
			,		
1	470	.4980	.0490	.6145	.6451
2	470	.5180	.0670	.6774	.7191
3	470	.6500	.0500	.7689	.8001
4	470	.7290	.0560	.8622	.8971
5	470	.7270	.0620	.8745	.9131
Ó	406	.3300	.0380	.4196	. 4451
, 1	406	.2750	.0290	.3434	.3629
8	406	.3670	.1060	.6170	.6882
9	406	.5700	.0430	.6714	.7003
10	406	.5180	.0570	.6524	.6907
11	448.	.6970	.0550	.8275	.8626
12	448	.7380	.0570	.8732	.9096
13	448	.9730	.0930	1.1936	1.2530
14	448	.3810	.0360	.4664	. 4894
15	448	.4180	.0430	.5200	.5475

## APPENDIX A

This appendix presents upper and lower confidence bounds of T for  $\alpha$  = .90, .95, .975, .99 and various sample sizes.

TABLE 11. UPPER AND LOWER CONFIDENCE BOUNDS OF T = (MU HAT - MU)/S(MU)

FOR ALPHA =0.91. 0.95. J.975. AND 0.99

p=.9

UPPER BOUND = (8+A\*Z)/(C\*(D+Z)). LOWER BOUND = (8-A\*Z)/(C\*(D-Z))

(Z VALUES ARE STANGARD NORMAL VALUES FOR ALPHA)

SAMPLE	ALPHA = 8.90	ALPHA = 8.95	ALPHA = 0.975	ALPHA = 0.99
SIZE	UPPER LOWER	UPPER LOWER	UPPER LOWER	UPPER LOWER
	BOUND BOUND	BOUND BOUND	BOUND BOUND	GUND BOUND
30	1.9409 -3.0236	2.2361 -3.8955	2.4825 -4.5783	2.7602 -5.6207
40	1.9798 -2.8941	2.2898 -3.6676	2.5504 -4.2996	2.8462 -5.2125
50	2.0079 -2.8137	2.3287 -3.4863	2.5997 -4.1339	2.9088 -4.9700
6 <b>0</b>	2.0296 -2.7580	2.3586 -3.4030	2.6378 -4.0160	2.9574 -4.8067
<b>61</b>	2.0315 -2.7533	2.3613 -3.3960	2.6411 -4.0065	2.9617 -4.7932
62	2.0333 -2.7468	2.3639 -3.3892	2.6444 -3.9972	2.9658 -4.7891
63	2.0352 -2.7444	2.3664 -3.3827	2.6476 -3.9882	2.9700 -4.7674
64	2.0370 -2.7401	2.3689 -3.3763	2.6508 -3.9795	2.9740 -4.7551
65	2.0387 -2.7359	2.3713 -3.3701	2.6539 -3.9710	2.9779 -4.7431
66	2.0404 -2.7319	2.3737 -3.3641	2.6569 -3.9627	2.9818 -4.7314
67	2.0421 -2.7279	2.376( -3.3582	2.6599 -3.9547	2.9856 -4.7201
68	2.0437 -2.7241	2.3783 -3.3525	2.6628 -3.9468	2.9893 -4.7091
69	2.0454 -2.7203	2.3805 -3.3469	2.6656 -3.9392	2.9929 -4.6984
70	2.0469 -2.7167	2.3827 -3.3415	2.6684 -3.9318	2.9965 -4.6880
71	2.0485 -2.7131	2.3849 -3.3362	2.6712 -3.9246	3.0000 -4.6778
72	2.0500 -2.7096	2.3871 -3.3311	2.6739 -3.9175	3.0035 -4.6679
73	2.0515 -2.7652	2.3891 -3.3268	2.6765 -3.9107	3.0069 -4.6583
74 75	2.0530 -2.7029	2.3911 -3.3211	2.6791 -3.9846	3.0102 -4.6489
75 76	2.0544 -2.6997 2.0559 -2.6965	2.3931 -3.3163 2.3951 -3.3116	2.6817 -3.8974	3.0135 -4.6397
77	2.0573 -2.6934	2.3978 -3.3171	2.6842 -3.8910	3.0167 -4.6308
78	2.0586 -2.6904	2.3989 -3.3026	2.6867 -3.8848 2.6891 -3.8787	3.0198 -4.6220 3.0230 -4.6135
79	2.0600 -2.6875	2.4008 -3.2982	2.6915 -3.8727	3.0250 -4.6152
80	2.0613 -2.6846	2.4026 -3.2939	2.6938 -3.8669	3.0290 -4.5970
81	2.0626 -2.6817	2.4045 -3.2898	2.6961 -3.8612	3.0320 -4.5891
82	2.0639 -2.6790	2.4962 -3.2857	2.6984 -3.8556	3.0349 -4.5813
93	2.6652 -2.6763	2.408# -3.2816	2.7007 -3.8502	3.0378 -4.5737
94	2.0664 -2.6736	2.4097 -3.2777		3.0406 -4.5662
85	2.0676 -2.6710	2.4114 -3.2739	2.7050 -3.8396	3.0433 -4.5590
36	2.0688 -2.6684	2.4131 -3.2701	2.7072 -3.8345	3.0461 -4.5518
87	2.0700 -2.6659	2.4147 -3.2664	2.7693 -3.8295	3.4488 -4.5448
88	2.0712 -2.6635	2.4164 -3.2628	2.7113 -3.8246	3.0514 -4.5380
89	2.0723 -2.6611	2.4186 -3.2593	2.7134 -3.8198	3.0540 -4.5313
90	2.0734 -2.6587	2.4195 -3.2558	2.7154 -3.8151	3.0566 -4.5247
91	2.0746 -2.6564	2.4211 -3.2524	2.7173 -3.8104	3.0592 -4.5183
92	2.0757 -2.6541	2.4226 -3.2490	2.7193 -3.3059	3.0617 -4.5120
93	2.1767 -2.6519	2.4241 -3.2458	2.7212 -3.8014	3.0641 -4.5058
94	2.0778 -2.6497	2.4256 -3.2425	2.7231 -3.7971	3.0665 -4.4997
95	2.0789 -2.6476	2.4271 -3.2394	2.7250 -3.7928	3.0689 -4.4937
100	2.0839 -2.6374	2.4341 -3.2244	2.7339 -3.7725	3.0805 -4.4655
120	2.1011 -2.6040	2.4580 -3.1754	2.7646 -3.7062	3.1198 -4.3738

TABLE 11.-CONTINUED

SAMPLE	ALPHA = 0.90	ALPHA = 0.95	ALPHA = 0.975	ALPHA = 0.99
SIZE	UPPER LOWER	UPPER LOWER	UPPER LOWER	UPPER LOWER
	BOUND BOUND	BOUND BOUND	BOUND BOUND	BOUND BOUND
140	2.1178 -2.5827	2.4806 -3.1432	2.7930 -3.6620	3.1558 -4.3119
160	2.1287 -2.5623	2.4959 -3.1137	2.8126 -3.6225	3.1812 -4.2577
180	2.1379 -2.5458	2.5086 -3.0897	2.8292 -3.5905	3.2027 -4.2141
200	2.1457 -2.5321	2.5199 -3.0699	2.8435 -3.5646	3.2212 -4.1779
220	2. 1526 -2. 5205	2.5295 -3.0531	2.8559 -3.5416	3.2373 -4.1474
240	2.1587 -2.5105	2.5380 -3.0386	2.8669 -3.5223	3.2515 -4.1213
260	2.1641 -2.5018	2.5456 -3.0260	2.8767 -3.5055	3.2642 -4.0985
2 90	2.1689 -2.4941	2.5524 -3.0149	2.8855 -3.4907	3.2757 -4.0785
300	2.1733 -2.4872	2.5586 -3.0050	2.8934 -3.4776	3.2860 -4.0607
320	2.1773 -2.4810	2.5642 -2.9961	2.9007 -3.4658	3-2955 -4-0448
348	2.1810 -2.4755	2.5694 -2.9381	2.9073 -3.4552	3.3042 -4.0304
360	2-1844 -2-4704	2.5741 -2.9868	2.9135 -3.4455	3.3121 -4.0173
380	2.1875 -2.4658	2.5785 -2.9741	2.9191 -3.4367	3.3195 -4.0054
400	2.1904 -2.4615	2.5826 -2.9680	2.9244 -3.4296	3.3264 -3.9945
420	2.1931 -2.4576	2.5864 -2.9624	2.9293 -3.4211	3.3328 -3.9844
440	2.1956 -2.4539	2.5899 -2.9571	2.9339 -3.4141	3.3388 -3.9751
460	2.1980 -2.4505	2.5933 -2.9523	2.9382 -3.4077	3.3444 -3.9664
480	2.2082 -2.4474	2.5964 -2.9477	2.9423 -3.4017	3.3497 -3.9583
500	2.2023 -2.4444	2.5994 -2.9435	2.9461 -3.3961	3.3547 -3.9507
520	2.2043 -2.4417	2.6022 -2.9395	2.9497 -3.3908	3.3594 -3.9437
548	2.2062 -2.4390	2.6048 -2.9358	2.9532 -3.3859	3.3639 -3.9370
560	2.2079 -2.4366	2.6073 -2.9322	2.9564 -3.3812	3.3681 -3.9387
5 8 <b>0</b>	2.2096 -2.4343	2.6097 -2.9289	2.9595 -3.3768	3.3722 -3.9248
600	2.2112 -2.4321	2.6126 -2.9257	2.9624 -3.3726	3.3760 -3.9192
620	2.2128 -2.4300	2.6141 -2.9227	2.9652 -3.3687	3.3797 -3.9139
640	2.2142 -2.4280	2.6162 -2.9199	2.9679 -3.3649	3.3832 -3.9089
66 <b>0</b>	2.2157 -2.4261	2.6182 -2.9172	2.9705 -3.3613	3.3865 -3.9041
680	2.2170 -2.4243	2.6201 -2.9146	2.9729 -3.3579	3.3897 -3.8995
700	2.2183 -2.4226	2.6219 -2.9121	2.9753 -3.3547	3.3928 -3.8951
720	2.2195 -2.4209	2.6236 -2.9198	2.9775 -3.3516	3.3958 -3.8989
740	2. 2207 -2. 41 93	2.6253 -2.9375	2.9797 -3.3486	3.3986 -3.8870
760	2.2219 -2.4178	2.6269 -2.9054	2.9818 -3.3457	3.4813 -3.8831
7 90	2.2230 -2.4164	2.6285 -2.9033	2.9838 -3.3430	3.4040 -3.8795
80 <u>0</u> ,	2.2240 -2.4150	2.6300 -2.9013	2.9858 -3.3404	3.4065 -3.8760
820	2.2250 -2.4137	2.6314 -2.8994	2.9876 -3.3379	3.4690 -3.8726
840	2.2260 -2.4124	2.6328 -2.8975	2.9894 -3.3354	3.4113 -3.8693 3.4136 -3.8662
860	2.2270 -2.4111	2.6342 -2.8958	2.9912 -3.3331	3.4158 -3.8632
880	2.2279 -2.4099	2.6355 -2.8941	2.9929 -3.3308 2.9945 -3.3287	3.4180 -3.8603
910	2.2288 -2.4088	2.6367 -2.8924	2.9945 -3.3287 2.9961 -3.3266	3.4200 -3.8574
920	2.2297 -2.4077	2.6380 -2.8908	2.9976 -3.3245	3.4220 -3.8547
940	2.2305 -2.4056	2.6391 -2.8893	E 3310 -3-3543	01455

TABLE 12. UPPER AND LOWER CONFIDENCE BOUNDS OF T = (MU HAT - MU)/S(MU)

FOR ALPHA =1.90, 0.95, 0.975, AND 0.99

P=.95

UPPER BCUND = (E+A\*Z)/(C\*(D+Z)), LOWER BOUND = (B+A\*Z)/(C\*(D-Z))

(Z VALUES ARE STANCARD NORMAL VALUES FOR ALPHA)

SAMPLE	ALPHA = 0.90	ALPHA = 1.95	ALPHA = 0.975	ALPHA = 0.99
SIZE	UPPER LOWER	UPPER LOWER	UPPER LOWER	UPPER LONER
	BOUND BOUND	BOUND BOUND	BOUND BOUND	BOUND BOUND
7.0	4 64 88 8 8 8 8 8 8 8 8			
36	1.9173 -2.9868	2.2088 -3.7591	2.4522 -4.5226	2.7265 -5.5522
46	1.9561 -2.8595	2.2623 -3.5645	2.5198 -4.2481	2.8121 -5.1501
50	1.9842 -2.7804	2.3011 -3.4450	2.5689 -4.0820	2.8744 -4.9112
6 <b>C</b>	2.0057 -2.7256	2.3309 -3.3636	2.6068 -3.9688	2.9226 -4.7502
6 <b>1</b> 62	2.0076 -2.7216	2.3335 -3.3561	2.6101 -3.9594	2.9269 -4.7369
6 <b>3</b>	2.0095 -2.7165	2.3361 -3.3495	2.6134 -3.9503	2.9310 -4.7240
64	2.0113 -2.7122	2.3386 -3.3430	2.6166 -3.9414	2.9351 -4.7115
65	2.0131 -2.7086 2.0148 -2.7039	2.3411 -3.3367 2.3435 -3.3386	2.6197 -3.9328	2.9391 -4.6993
66	2.0165 -2.6999	2.3458 -3.3247	2.6228 -3.9244	2.9433 -4.6875
67	2.0182 -2.6960	2.3482 -3.3189	2.6258 -3.9163 2.6287 -3.9084	2.9468 -4.6760
68	2.0198 -2.6922	2.3504 -3.3133	2.6316 -3.9007	2.9506 -4.6649
69	2.0214 -2.6885	2.3527 -3.3078	2.6344 -3.8932	2.9543 -4.6540
70	2.0230 -2.6849	2.3548 -3.3024	2.6372 -3.8859	2.9579 -4.6435 2.9615 -4.6332
71	2.0246 -2.6814	2.3570 -3.2972	2.6400 -3.8787	2.9650 -4.6232
72	2.0261 -2.6780	2.3591 -3.2922	2.6426 -3.8718	2.9684 -4.6134
73	2.6276 -2.6747	2.3612 -3.2872	2.6453 -3.8650	2.9718 -4.6039
74	2.0290 -2.6714	2.3632 -3.2824	2.6479 -3.8584	2.9751 -4.5947
75	2.4305 -2.6682		2.6504 -3.8520	2.9783 -4.5856
76	2.0319 -2.6651	2.3672 -3.2730	2.6529 -3.8457	2.9815 -4.5768
77	2.0333 -2.6620	2.3691 -3.2685	2.6553 -3.8395	2.9846 -4.5682
78	2.0346 -2.6591	2.3710 -3.2641	2.6578 -3.8335	2.9877 -4.5598
79	2.0360 -2.6562	2.3728 -3.2598	2.6601 -3.8276	
80	2.0373 -2.6533	2.3747 -3.2556	2.6625 -3.8219	2.9937 -4.5435
81	2.0386 -2.6505	2.3765 -3.2515	2.6648 -3.8163	2.9967 -4.5357
82	2.6399 -2.6478	2.3782 -3.2474	2.6670 -3.8108	2.9996 -4.5280
83	2.0411 -2.6451	2.3801 -3.2435	2.6692 -3.8054	3.0024 -4.5205
84	2.0424 -2.6425	2.3817 -3.2396	maa.	3.0052 -4.5131
85	2.0436 -2.6486		2.6736 -3.7950	3.0080 -4.5060
86	2.8448 -2.6374	2.3850 -3.2321	2.6757 -3.7906	3.0107 -4.4989
97	2.0459 -2.6350	2.3867 -3.2285	2.6778 -3.7850	3.0133 -4.4920
88	2.0471 -2.6326	2.3883 -3.2249	2.6798 -3.7802	3.0160 -4.4853
89 90	2.0482 -2.6302	2.3899 -3.2214	2.6819 -3.7754	3.0186 -4.4787
9 <b>0</b> 9 <b>1</b>	2.0494 -2.6279 2.0505 -2.6256	2.3914 -3.2180		3.0211 -4.4722
92	2.0516 -2.6234	2.3930 -3.2146 2.3945 -3.2114	2.6858 -3.7662	3.0236 -4.4658
93	2.0527 -2.6212	2.3960 -3.2081	2.6877 -3.7617 2.6897 -3.7574	3.0261 -4.4596
94	2.6537 -2.6190	2.3975 -3.2049	2.6915 -3.7530	3.0286 -4.4535 3.0310 -4.4475
95	2.0548 -2.6159	2.3989 -3.2018	2.6934 -3.7488	3.0334 -4.4416
100	2.0598 -2.6069	2.4059 -3.1871	2.7023 -3.7238	3.0448 -4.4138
120	2. 1769 -2. 5740	2.4297 -3.1387	2.7327 -3.6635	3.0838 -4.3234
			E-10E1 010000	044000 -400504

SAMPLE	ALPHA = 0.90	ALPHA = \$.95	ALPHA = 0.975	ALPHA = 0.99
SIZE	UPPER LOWER	UPPER LOWER	UPPER LOWER	UPPER LOWER
	BOUND BOUND	BOUND BOUND	60 UND BOUND	BOUND BOUND
140	2.0938 -2.5534	2.4525 -3.1076	2.7613 -3.6206	3.1200 -4.2631
160	2.1046 -2.5333	2.4676 -3.0784	2.7807 -3.5814	3.1452 -4.2095
1.30	2.1136 -2.5170	2.4804 -3.0549	2.7972 -3.5498	3.1664 -4.1663
200	2.1214 -2.5035	2.4913 -3.0351	2.8113 -3.5236	3.1847 -4.1306
228	2.1282 -2.4920	2.5009 -3.0185	2.8235 -3.5015	3.2006 -4.1005
240	2.1342 -2.4821	2.5093 -3.0042	2.8344 -3.4824	3.2147 -4.0746
260	2.1396 -2.4734	2.5168 -2.9917	2.8441 -3.4658	3.2273 -4.0521
280	2.1444 -2.4658	2.5235 -2.9807	2.8528 -3.4512	3.2386 -4.0323
330	2.1487 -2.4590	2.5296 -2.9710	2.8607 -3.4382	3.2488 -4.0147
320	2.1527 -2.4529	2.5352 -2.9622	2.8678 -3.4266	3.2582 -3.9990
340	2.1563 -2.4474	2.5403 -2.9543	2.8744 -3.4161	3.2667 -3.9848
360	2.1596 -2.4424	2.5450 -2.9471	2.8805 -3.4065	3.2746 -3.9719
380	2.1627 -2.4379	2.5493 -2.9405	2.8861 -3.3978	3.2820 -3.9601
400	2.1656 -2.4336	2.5534 -2.9344	2.8913 -3.3897	3.2887 -3.9493
420	2.1683 -2.4298	2.5571 -2.9288	2.8962 -3.3823	3.2951 -3.9393
440	2.1708 -2.4262	2.560£ +2.9237	2.9017 -3.3755	3.3010 -3.9301
460	2.1731 -2.4228	2.5639 -2.9189	2.9050 -3.3691	3.3066 -3.9215
480	2.1753 -2.4197	2.5670 -2.9144	2.9090 -3.3632	3.3118 -3.9135
50 <b>0</b>	2.1774 -2.4168	2.5699 -2.9162	2.9128 -3.3576	3.3167 -3.9060
520	2.1793 -2.4140	2.5727 -2.9062	2.9163 -3.3524	3.3214 -3.8990
540	2.1812 -2.4114	2.5,53 -2.9025	2.9197 -3.3475	3.3258 -3.8924
56 <b>0</b>	2.1829 -2.4094	2.5778 -2.8990	2.9229 -3.3429	3.3300 -3.8862
580	2.1846 -2.4067	2.5802 -2.8957	2.9260 -3.3386	3.3340 -3.8804
6 <b>00</b>	2.1862 -2.4845	2.5824 -2.8926	2. 92 89 -3. 3344	3.3378 -3.8748
620	2.1877 -2.4025	2.5846 -2.8897	2.9317 -3.3305	3.3414 -3.8696
640	2.1892 -2.4005	2.5866 -2.8868	2.9343 -3.3268	3.3449 -3.8646
66 <b>0</b>	2.1906 -2.3986	2.5886 -2.8842	2.9369 -3.3233	3.3482 -3.8599 3.3514 -3.8553
6 9 0	2.1919 -2.3968	2.5904 -2.8816	2.9393 +3.3199	
700	2.1932 -2.3951	2.5922 -2.8792	2.9416 -3.3167 2.9438 -3.3136	3.3544 -3.8510 3.3573 -3.8469
720	2.1944 -2.3935	2.5939 -2.8768		3.3601 -3.8430
740	2.1956 -2.3920	2.5956 -2.8746		3.3628 -3.8392
768	2.1967 -2.3965	2.5972 -2.8725		3.3654 -3.8356
780	2.1978 -2.3890	2.5987 -2.8704	2.9500 -3.3052 2.9520 -3.3026	3.3679 -3.8321
8 0.0	2.1988 -2.3877	2.6002 -2.8685		3.3784 -3.8287
82 <b>0</b>	2.1999 -2.3863	2.6016 -2.8666	2.9538 -3.3091 2.9556 -3.2977	3.3727 -3.8255
840	2.2008 -2.3851	2.6030 -2.8647	2.9573 -3.2954	3.3750 -3.8224
860	2.2018 -2.3838	2.6044 -2.8630 2.6056 -2.8613	2.9598 -3.2931	3.3772 -3.8194
880	2.2027 -2.3827	2.6169 -2.8597	2.9606 -3.2910	3.3793 -3.8166
900	2.2036 -2.3815 2.2044 -2.3804	2.6081 -2.8581	2.9622 -3.2839	3.3813 -3.8138
920		2.6093 -2.8566	2.9637 -3.2869	3.3833 -3.8111
948	2.2053 -2.3794	E 6 0 9 2 - E 6 0 9 C D	E# 3001 - 0# E003	J10000 010222

TABLE 13. UPPER AND LOWER CONFIDENCE BOUNDS OF T = (MU HAT - MU)/S(MU)

FOR ALPHA =0.91. 0.95. 0.975. AND 0.99

p=.975

UPPER BOUND = (8+A\*Z)/(C\*(D+Z)), LOWER BOUND = (8-A\*Z)/(C\*(D-Z))

(Z VALUES ARE STANCARD NORMAL VALUES FOR ALPHA)

SAMPLE	ALPHA = 0.90	ALPHA = 0.95	ALPHA = 0.975	ALPHA = C.99
SIZE	UPPER LOWER	UPPER LOWER	UPPER LOWER	UPPER LOWER
01	BOUND BOUND	BOUND BOUND	BOUND BOUND	BOUND BOUND
70	4 0007 0 0405	0.4007 7.7440	0 2022 6 2066	0 6 64 5 5 4 044
30	1.8927 -2.9485	2.1805 -3.7118	2.4207 -4.4646	2.6915 +5.4811
48	1.9313 -2.8233	2.2337 -3.5193	2.4879 -4.1943 2.5366 -4.0307	2.7764 -5.0849 2.8382 -4.8494
50	1.9592 -2.7454	2.2721 -3.4817 2.3017 -3.32(9	2.5741 -3.9191	2.8860 -4.6937
60	1.9866 -2.6915 1.9825 -2.6869	2.3043 -3.3141	2.5774 -3.9099	2.8902 -4.6776
61 62	1.9843 -2.6825	2.3068 -3.3075	2.5807 -3.9008	2.8943 -4.6649
63	1. 9861 -2.6783	2.3093 -3.3012	2.5838 -3.8921	2.8984 -4.6525
64	1.9879 -2.6741	2.3118 -3.2950	2.5869 -3.8836	2.9023 -4.6405
65	1.9896 -2.6761	2.3142 -3.2890	2.5900 -3.8754	2.9062 -4.6289
66	1.9913 -2.6661	2.3165 -3.2931	2.5929 -3.8673	2.9100 -4.6176
67	1.9930 -2.6623	2.3188 -3.2774	2.5959 -3.8595	2.9137 -4.6066
68	1.9946 -2.6586	2.3211 -3.2719	2.5987 -3.8519	2.9174 -4.5959
69	1.9962 -2.6550	2.3233 -3.2665	2.6015 -3.8445	2.9210 -4.5855
70	1.9977 -2.6514	2.3254 -3.2612	2.6043 -3.8373	2.9245 -4.5753
71	1.9993 -2.6484	2.3276 -3.2561	2.6070 -3.8303	2.9279 -4.5655
72	2.00082.6446	2.3297 -3.2511	2.6097 -3.8235	2.9313 -4.5559
73	2.0923 -2.6413	2.3317 -3.2462	2.6123 -3.8168	2.9347 -4.5465
74	2.0037 -2.6381	2.3337 -3.2414	2.6148 -3.8103	2.9379 -4.5373
75	2.0051 -2.6349	2.3357 -3.2368	2.6173 -3.3039	2.9412 -4.5284
76	2.0065 -2.6319	2.337 c -3.232?	2.6198 -3.7977	2.9443 -4.5197
. 77	2.0079 -2.6239	2.3395 -3.2278	2.6222 -3.7917	2.9474 -4.5112
78	2.0093 -2.6259	2.3414 -3.2234	2.6246 -3.7857	2.9505 -4.5029
79	2.[106 -2.6231	2.3433 -3.2192	2.6270 -3.7800 2.6293 -3.7743	2.9535 -4.4948 2.9564 -4.4869
30	2,0119 -2.6203	2.3451 -3.2158 2.3469 -3.2110	2.6316 -3.7688	2.9594 -4.4792
8 <b>1</b> 82	2.0132 -2.6175 2.0145 -2.6148	2.3486 -3.2070	2.6338 -3.7633	2.9622 -4.4716
93	2.0157 -2.6122	2.3503 -3.2331	2.6369 -3.7580	2.9650 -4.4642
84	2.0169 -2.6096	2.3526 -3.1993	2.6382 -3.7529	2.9678 -4.4570
85	2.0181 -2.6071	2.3537 -3.1956	2.6403 -3.7478	2.9705 -4.4499
86	2.0193 -2.6046	2.3554 -3.1919	2.6424 -3.7428	2.9732 -4.4430
37	2.0205 -2.6022	2.3571 -3.1983	2.6445 -3.7379	2.9759 -4.4362
38	2.0216 -2.5998	2.3586 -3.1848	2.6465 -3.7332	2.9785 -4.4295
39	2.0228 -2.5975	2.3601 -3.1814	2.6485 -3.7285	2.9818 -4.4238
90	2.0239 -2.5952	2.3617 -3.1780	2.6505 -3.7239	2.9836 -4.4166
91	2.0250 -2.5930	2.3632 -3.1747	2.6524 -3.7194	2.9861 -4.4103
92	2.0261 -2.5908	2.3647 -3.1714	2.6543 -3.7150	2.9885 -4.4042
93	2.6271 -2.5886	2.3662 -3.1683	2.6562 -3.7107	2.9909 -4.3982
94	2. u 282 -2.5865	2.3677 -3.1651	2.6581 -3.7064	2.9933 -4.3923
95	2.0292 -2.5844	2.3691 -3.1621	2.6599 -3.7023	2.9957 -4.3865
100	2.0342 -2.5745	2.3761 -3.1475	2.6687 -3.6825	3.0070 -4.3590
120	2.0512 -2.5421	2.3996 -3.4999	2.6988 -3.6181	3.0456 -4.2699

TABLE 13.-CONTINUED

CAMBLE	AL DUA - 0 00	11 DUA 0 OF		
SAMPLE	ALPHA = 0.90	ALPHA = C.95	ALPHA = 0.975	ALPHA = 0.99
SIZE	UPPER LOWER	UPPER LOWER	UPPER LOWER	UPPER LOWER
	BOUND BOUND	BOUND BOUND	BOUND BOUND	BOUND BOUND
140	2.0681 -2.5222	2.4225 -3.0696	2.7275 -3.5763	3.0818 -4.2109
160	2.0788 -2.5023	2.4374 -3.0467	2.7467 -3.5376	3.1066 -4.1580
180	2.0878 -2.4862	2.4500 -3.0174	2.7629 -3.5864	3.1276 -4.1153
200	2.0955 -2.4728	2.4608 -2.9980	2.7768 -3.4895	3.1457 -4.0801
220	2.1022 -2.4615	2.4702 -2.9816	2.7890 -3.4586	3.1614 -4.0503
240	2.1981 -2.4517	2.4786 -2.9674	2.7997 -3.4398	3.1754 -4.0247
260	2.1134 -2.4432	2.4860 -2.9551	2.8093 -3.4234	3.1878 -4.0025
2 3 0	2.1181 -2.4356	2.4926 -2.9443	2.8179 -3.4096	3.1989 -3.9830
300 320	2.1224 -2.4289	2.4987 -2.9346 2.5041 -2.9259	2.8256 -3.3961	3.2091 -3.9656
340	2.1263 -2.4229 2.1299 -2.4175	2.5041 -2.9259 2.5092 -2.9181	2.8327 -3.3846 2.8392 -3.3742	3.2183 -3.95#0 3.2268 -3.9360
360	2.1332 -2.4125	2.5138 -2.9110	2.8452 -3.3648	3.2346 -3.9232
3.80	2.1362 -2.4080	2.5181 -2.9945	2.8508 -3.3562	3.2418 -3.9116
490	2.1391 -2.4039	2.5221 -2.8985	2.8559 -3.3483	3.2485 -3.9009
420	2.1417 -2.4000	2.5258 -2.8930	2.8607 -3.3409	3.2547 -3.8911
440	2.1442 -2.3965	2.5293 -2.8879	2.8652 -3.3342	3.2606 -3.8820
460	2.1465 -2.3932	2.5325 -2.8831	2.8694 -3.3279	3.2661 -3.8735
480	2.1487 -2.3981	2.5356 -2.8787	2.8734 -3.3220	3.2713 -3.8656
500	2.1507 -2.3872	2.5385 -2.8745	2.8771 -3.3165	3.2761 -3.8582
52 <b>0</b>	2.1527 -2.3845	2.5412 -2.8707	2.8806 -3.3114	3.2807 -3.8513
540	2.1545 -2.3819	2.5438 -2.8670	2.8840 -3.3066	3.2851 -3.8448
560	2.1562 -2.3795	2.5462 -2.8635	2.8872 -3.3020	3.2892 -3.8387
580	2.1579 -2.3772	2.5486 -2.8603	2.8902 -3.2977	3.2932 -3.8329
600	2.1595 -2.3751	2.5508 -2.8572	2.8930 -3.2936	3.2969 -3.8274
62 <b>0</b> 640	2.1619 -2.3731 2.1624 -2.3711	2.5529 -2.8543	2.8958 -3.2898	3.3005 -3.8222
660	2.1638 -2.3693	2.5549 -2.8515 2.5569 -2.8489	2.8984 -3.2861 2.9009 -3.2826	3.3039 -3.8173 3.3072 -3.8126
68 <b>0</b>	2.1651 -2.3675	2.5587 -2.8463	2.9033 -3.2793	3.3103 -3.8081
700	2.1663 -2.3658	2.5605 -2.8439	2.9056 -3.2761	3.3133 -3.8039
720	2.1675 -2.3642	2.5622 -2.8416	2.9078 -3.2731	3.3162 -3.7998
740	2.1687 -2.3627	2.5638 -2.8394	2.9099 -3.2702	3.3190 -3.7959
760	2.1698 -2.3612	2.5654 -2.8373	2.9120 -3.2674	3.3217 -3.7922
780	2.1709 -2.3598	2.5669 -2.8353	2.9139 -3.2647	3.3242 -3.7886
890	2.1719 -2.3584	2.5684 -2.8333	2.9158 -3.2621	3.3267 -3.7852
820	2.1729 -2.3571	2.5698 -2.8315	2. 9177 -3. 2597	3.3291 -3.7819
840	2.1739 -2.3559	2.5712 -2.8297	2.9194 -3.2573	3.3314 -3.7787
860	2.1748 -2.3547	2.5725 -2.8279	2.9211 -3.2550	3.3337 -3.7756
890	2.1757 -2.3535	2.5738 -2.8263	2.9228 -3.2528	3.3358 -3.7727
900	2.1766 -2.3524	2.5750 -2.8247	2.9244 -3.2507	3.3379 -3.7698
928	2.1775 -2.3513	2.5762 -2.8231	2. 92 59 - 3. 2486	3.3399 -3.7671
940	2.1783 -2.3502	2.5773 -2.8216	2.9274 -3.2467	3.3419 -3.7644

TABLE 14. UPPER AND LOWER CONFIDENCE BOUNDS OF T = (MU HAT - MU)/S(MU)

FOR ALPHA = 0.96, 0.95, 0.975, AND 0.99

p=.99

UPPER BCUND = (E+A\*Z)/(C\*(D+Z)), LOWER BCUND = (B-A\*Z)/(C\*(D-Z))

(Z VALUES ARE STANDARD NORMAL VALUES FOR ALPHA)

SAMPLE	ALPHA = 0.90	ALPHA = 8.95	ALPHA = 6.975	ALPHA = G.99
SIZE	UPPER LOWER	UPPER LOWER	UPPER LOWER	UPPER LOWER
	BOUND BOUND	BOUND BOUND	BOUND BOUND	BOUND BOUND
30	1.8626 -2.9017	2.1458 -3.6520	2.3823 -4.3937	2.6488 -5.3940
40	1.9008 -2.7758	2.1984 -3.4638	2.4487 -4.1282	2.7326 -5.0047
50	1.9284 -2.7023	2.2364 -3.3483	2.4967 -3.9674	2.7936 -4.7733
60	1.9496 -2.6493	2.2657 -3.2689	2.5338 -3.8578	2.8408 -4.6173
6 <b>1</b>	1.9514 -2.6449	2.2682 -3.2623	2.5371 -3.8487	2.8450 -4.6044
62	1.9533 -2.6446	2.2707 -3.2558	2.5403 -3.8398	2.8490 -4.5919
63	1.9550 -2.6364	2.2732 -3.2496	2.5434 -3.8313	2.8530 -4.5798
64	1.9568 -2.6323	2.2756 -3.2435	2.5465 -3.8229	2.8569 -4.5680
65	1.9585 -2.6283	2.2784 -3.2376	2.5495 -3.8148	2.8608 -4.5565
66	1.9602 -2.6245	2.2803 -3.2318	2.5524 -3.8069	2.8645 -4.5454
67	1.9518 -2.6247	2.2826 -3.2262	2.5553 -3.7992	2.8682 -4.5346
68	1.9634 -2.6171	2.2848 -3.2268	2.5581 -3.7918	2.8718 -4.5241
69	1.9650 -2.6135	2.2871 -3.2155	2.5609 -3.7845	2.8753 -4.5139
70	1.9665 -2.6100	2.2891 -3.2103	2.5636 -3.7774	2.8788 -4.5039
71 72	1.9681 -2.6066	2.2912 -3.2053	2.5663 -3.7795	2.8822 -4.4942
72	1.9695 +2.6033	2.2933 -3.2063	2.5689 -3.7638	2.8856 -4.4848
73 74	1.9710 -2.6031 1.9724 -2.5969	2.2953 -3.1955	2.5715 -3.7572	2.8889 -4.4755
75	1.9739 -2.5938	2.2973 -3.1969 - 2.2992 -3.1863	2.5740 -3.7508	2.8921 -4.4666
76	1.9752 -2.5908	2.3012 -3.1818	2.5765 -3.7446 2.5789 -3.7385	2.8953 -4.4578
77	1.9766 -2.5879	2.3031 -3.1774	2.5813 -3.7325	2.8984 -4.4492 2.9015 -4.4409
78	1.9779 -2.5850	2.3049 -3.1732	2.5837 -3.7267	2.9045 -4.4327
79	1.9793 -2.5822	2.3067 -3.1699	2.5860 -3.7210	2.9074 -4.4248
3 Ú	1.9805 -2.5794	2.3085 -3.1649	2.5883 -3.7155	2.9104 -4.4170
91	1.9818 -2.5767	2.3103 -3.1669	2.5905 -3.7110	2.9132 -4.4094
82	1.9831 -2.5741	2.312( -3.1570	2.5928 -3.7047	2.9160 -4.4019
83	1.9843 -2.5715	2.3137 -3.1532	2.5949 -3.6995	2.9188 -4.3947
34	1.9855 -2.5690	2.3154 -3.1495	2.5971 -3.6944	2.9216 -4.3875
85	1. 9867 -2.5665	2.3170 -3.1458	2.5992 -3.6894	2.9243 -4.3806
86	1.9879 -2.5641	2.3187 -3.1422	2.6012 -3.6845	2.9269 -4.3738
87	1.9890 -2.5617	2.3203 -3.1387	2.6033 -3.6797	2.9295 -4.3671
88	1.9902 -2.5593	2.3218 -3.1352	2.6053 -3.6750	2.9321 -4.3605
89	1.9913 -2.5571	2.3234 -3.1319	2.6073 -3.6704	2.9346 -4.3541
90	1. 9924 -2.5548	2.3249 -3.1285	2.6092 -3.6659	2.9371 -4.3478
91	1.9935 -2.5526	2.3264 -3.1253	2.6111 -3.6615	2.9396 -4.3417
92	1.9945 -2.5504	2.3279 -3.1221	2.6130 -3.6572	2.9420 -4.3356
93	1.9956 -2.5483	2.3294 -3.1193	2.6149 -3.6529	2.9444 -4.3297
94	1.9966 -2.5462	2.3308 -3.1159	2.6167 -3.6487	2.9467 -4.3239
95	1.9977 -2.5442	2.3322 -3.1129	2.6185 -3.6446	2.9491 -4.3182
100	2.0026 -2.5345	2.3391 -3.0985	2.6272 -3.6252	2.9602 -4.2913
120	2.0193 -2.5026	2.3623 -3.0517	2.6569 -3.5619	2.9984 -4.2036

SAMPLE	ALPHA = 0.90	ALPHA = £.95	ALPHA = 0.975	ALPHA = 0.99
SIZE	UPPER LOWER	UPPER LOWER	UPPER LOWER	UPPER LOWER BOUND
140	2.0363 -2.4833	2.3852 -3.0223	2.6855 -3.5212	3.0344 -4.1461
160	2.0468 -2.4638	2.3999 -2.9939	2.7044 -3.4831	3.0588 -4.0940
180	2.0556 -2.4479	2.4123 -2.9709	2.7204 -3.4524	3.0795 -4.0520
200	2.0632 -2.4347	2.4229 -2.9518	2.7341 -3.4269	3.0972 -4.0172
220	2.0698 -2.4236	2.4322 -2.9357	2.7460 -3.4053	3.1128 -3.9879
240	2.0756 -2.4139	2.4404 -2.9217	2.7566 -3.3868	3.1265 -3.9628
260	2.0808 -2.4055	2.4477 -2.9J96	2.7660 -3.3707	3.1387 -3.9409
280	2.0855 -2.3981	2.4542 -2.8989	2.7745 -3.3565	3.1497 -3.9216
300	2.0897 -2.3915	2.4602 -2.8894	2.7821 -3.3438	3.1596 -3.9045
320	2.0936 -2.3856	2.4656 -2.8819	2.7891 -3.3325	3.1687 -3.8892
340	2.0971 -2.3802	2.4705 -2.8732	2.7955 -3.3223	3.1771 -3.8754
360	2.1003 -2.3754	2.4751 -2.8662	2.8014 -3.3130	3.1847 -3.8628
380	2.1033 -2.3769	2.4793 -2.8597	2.8069 -3.3045	3.1918 -3.8514
400	2.1061 -2.3668	2.4832 -2.8539	2.8119 -3.2967	3.1984 -3.8408
420	2.1087 -2.3631	2.4869 -2.8484	2.8167 -3.2895	3.2046 -3.8311
440	2.1111 -2.3595	2.4903 -2.8434	2.8211 -3.2828	3.2104 -3.8222
460	2.1134 -2.3563	2.4935 -2.8387	2.8252 -3.2766	3.2158 -3.8138
480	2.1156 -2.3533	2.4965 -2.8344	2.8291 -3.2719	3.2209 -3.8061
5 <b>00</b>	2.1176 -2.3504	2.4994 -2.8303	2.8328 -3.2655	3.2257 -3.7988
520 540 568 580 600 620	2.1195 -2.3477 2.1213 -2.3452 2.1230 -2.3429 2.1246 -2.3406 2.1262 -2.3385 2.1277 -2.3365 2.1291 -2.3346	2.5021 -2.8264 2.5046 -2.8228 2.5070 -2.8194 2.5093 -2.8162 2.5115 -2.8132 2.5136 -2.8103 2.5156 -2.8076	2.8363 -3.2604 2.8396 -3.2556 2.8427 -3.2512 2.8457 -3.2469 2.8485 -3.2429 2.8512 -3.2391 2.8538 -3.2355	3.2302 -3.7920 3.2345 -3.7856 3.2386 -3.7795 3.2425 -3.7739 3.2461 -3.7685 3.2497 -3.7634 3.2530 -3.7585
660	2.1291 -2.3328	2.5175 -2.8050	2.8562 -3.2320	3.2563 -3.7539 3.2593 -3.7495 3.2623 -3.7453 3.2651 -3.7413 3.2679 -3.7375 3.2705 -3.7338
690	2.1317 -2.3310	2.5193 -2.8025	2.8586 -3.2288	
700	2.1338 -2.3294	2.5211 -2.8001	2.8608 -3.2256	
720	2.1342 -2.3278	2.5227 -2.7979	2.8630 -3.2226	
740	2.1353 -2.3263	2.5243 -2.7957	2.8651 -3.2198	
760	2.1364 -2.3248	2.5259 -2.7936	2.8671 -3.2170	
780 800 820 848 860 880	2.1375 -2.3234 2.1385 -2.3221 2.1395 -2.3208 2.1404 -2.3196 2.1413 -2.3184 2.1422 -2.3172 2.1431 -2.3161	2.5274 -2.7916 2.5288 -2.7897 2.5302 -2.7879 2.5316 -2.7861 2.5329 -2.7844 2.5341 -2.7827 2.5353 -2.7812	2.8690 -3.2144 2.8709 -3.2119 2.8727 -3.2095 2.8745 -3.2071 2.8761 -3.2049 2.8778 -3.2027 2.8793 -3.2006	3.2730 -3.7303 3.2755 -3.7269 3.2778 -3.7236 3.2801 -3.7205 3.2823 -3.7175 3.2844 -3.7146 3.2865 -3.7118
92 <b>0</b>	2.1439 -2.3151	2.5365 -2.7796	2.8809 -3.1986	3.2885 -3.7091
94 <b>0</b>	2.1447 -2.3140	2.5376 -2.7781	2.8823 -3.1967	3.2904 -3.7065

TABLE 15. UPPER AND LOWER CONFIDENCE BOUNDS OF T = (MU HAT - MU)/S(MU)

FOR ALPHA =0.90, 0.95, 0.975, AND 0.99

p=.995

UPPER BCUND = (8+A\*Z)/(C\*(D+Z)), LOWER BOUND = (8-A\*Z)/(C\*(D-Z))

(Z VALUES ARE STANDARD NORMAL VALUES FOR ALPHA)

		:		
SAMPLE	ALPHA = 0.90	ALPHA = C.95	ALPHA = 0.975	ALPHA = 0.99
SIZE	UPPER LOWER	UPPER LOWER	UPPER LOWER	UPPER LOWER
	BOUND BOUND	BOUND BOUND	BOUND BOUND	BOUND BOUND
	355.,5		200112	333,13
30	1.8422 -2.8700	2.1224 -3.6122	2.3562 -4.3458	2.6198 -5.3351
40	1.8892 -2.7486	2.1746 -3.4262	2.4221 -4.0834	2.7630 -4.9584
<b>50</b>	1.9075 -2.6731	2.2122 -3.3121	2.4697 -3.9245	2.7634 -4.7216
6 <b>0</b>	1.9285 -2.6208	2.2412 -3.2336	2.5065 -3.8162	2.8101 -4.5675
61	1.9304 -2.6164	2.2438 -3.2271	2.5097 -3.8072	2.8143 -4.5548
62	1.9322 -2.6121	2.2462 -3.2267	2.5129 -3.7984	2.8183 -4.5424
63	1.9339 -2.6080	2.2487 -3.2145	2.5160 -3.7899	2.8222 -4.5304
64	1.9357 -2.6039	2.2511 -3.2385	2.5190 -3.7817	2.8261 -4.5187
65	1.9374 -2.6000	2.2534 -3.2027	2.5220 -3.7737	2.8299 -4.5074
66	1.9390 -2.5962	2.2557 -3.1979	2.5249 -3.7659	2.8336 -4.4964
67	1.9407 -2.5925	2.2580 -3.1915	2.5277 -3.7583	2.8373 -4.4857
68	1.9422 -2.5889	2.2692 -3.1861	2.5346 -3.7509	2.8408 -4.4753
69	1.9438 -2.5853	2.2623 -3.1808	2.5333 -3.7437	2.8444 -4.4652
78	1.9453 -2.5819	2.2645 -3.1757	2.5360 -3.7367	2.8478 -4.4554
71	1.94692.5785	2.2665 -3.1717	2.5386 -3.7299	2.8512 -4.4458
72	1.9483 -2.5753	2.2686 -3.1659	2.5412 -3.7233	2.8545 -4.4364
73	1.9498 -2.5721	2.2706 -3.1611	2.5438 -3.7168	2.8577 -4.4273
74	1.9512 -2.5691	2.2726 -3.1565	2.5463 -3.7105	2.8609 -4.4185
75	1.9526 -2.5659	2.2745 -3.1520	2.5488 -3.7043	2.8641 -4.4098
76	1.9540 -2.5629	2.2764 -3.1476	2.5512 -3.6982	2.8672 -4.4013
77	1.9553 -2.5600	2.2783 -3.1432	2.5535 -3.6924	2.8702 -4.3931
78	20 7700 277712	2.2801 -3.1390	2.5559 -3.6866	2.8732 -4.3850
79	1.9579 -2.5544	2.2819 -3.1349	2.5582 -3.6816	2.8761 -4.3772
80	1.9592 -2.5517	2.2537 -3.1309	2.5604 -3.6755	
91	1.9605 -2.5490	2.2854 -3.1269	2.5627 -3.6731	2.8819 -4.3619
82	1.9617 -2.5464	2.2871 -3.1231	2.5649 -3.6648	2.8847 -4.3546
93	1.9629 -2.5438	2.2888 -3.1193	2.5679 -3.6597	2.8874 -4.3474
84	1.9641 -2.5413	2.2905 -3.1156	2.5691 -3.6547	2.8961 -4.3404
85	1.9653 -2.5389	2.2921 -3.1128	2.5712 -3.6497	2.8928 -4.3335
86	1.9665 -2.5365	2.2937 -3.1084	2.5733 -3.6449	2.8954 -4.3267
87	1.9676 -2.5341	2.2953 -3.1049		2.8989 -4.3201
58	1.9688 -2.5318	2.2969 -3.1015	2.5773 -3.6355	2.9006 -4.3136
89	1.9699 -2.5296	2.2984 -3.0982	2.5792 -3.6310	2.9031 -4.3073
90	1.9710 -2.5273	2.2999 -3.0949	2.5812 -3.6265	2.9055 -4.3011
91	1.9720 -2.5252	2.3014 -3.0917	2.5831 -3.6222	2.9080 -4.2950
92	1.9731 -2.5230	2.3029 -3.0885	2.5849 -3.6179	2.9104 -4.2890
93	1.9741 -2.5209	2.3043 -3.0854	2.5868 -3.6137	2.9127 -4.2832
94	1.9752 -2.5189	2.3058 -3.0824	2.5886 -3.6095	2.9151 -4.2774
95	1.9762 -2.5168	2.3072 -3.0794	2.5904 -3.6055	2.9174 -4.2718
100	1.9810 -2.5072	2.3139 -3.0653	2.5990 -3.5863	2.9284 -4.2452
120	1.9976 -2.4758	2.3370 -3.0190	2.6284 -3.5237	2.9662 -4.1585

TABLE 15 .- CONTINUED

SAMPLE	ALPHA = 0.90	ALPHA = 0.95	ALPHA = 0.975	ALPHA = 0.99
SIZE	UPPER LOWER	UPPER LOWER	UPPER LOWER	UPPER LOWER BOUND
1 40	2.0146 -2.4569	2.3597 -2.9961	2.6569 -3.4837	3.0020 -4.1019
160	2.0249 -2.4375	2.3743 -2.9620	2.6756 -3.4460	3.0262 -4.0503
180	2.0337 -2.4218	2.3865 -2.9392	2.6913 -3.4156	3.0466 -4.0088
200	2.9412 -2.4088	2.3971 -2.9204	2.7649 -3.3904	3.0642 -3.9744
200	2.9477 -2.3977	2.4063 -2.9044	2.7167 -3.3690	3.0796 -3.9454
2 48	2.0535 -2.3882	2.4144 -2.8906	2.7272 -3.3507	3.0931 -3.9205
2 6 <b>0</b>	2.0586 -2.3799	2.4216 -2.8786	2.7365 -3.3347	3.1652 -3.8989
2 80	2.0633 -2.3726	2.4281 -2.8680	2.7449 -3.3207	3.1161 -3.8798
300	2.0674 -2.3660	2.4339 -2.8586	2.7524 -3.3682	3.1259 -3.8629
320	2.0712 -2.3602	2.4393 -2.8502	2.7594 -3.2970	3.1349 -3.8477
348	2.0747 -2.3549	2.4442 -2.8425	2.7657 -3.2868	3.1432 -3.8340
360	2.0779 -2.3500	2.4487 -2.8356	2.7715 -3.2776	3.1508 -3.8216
380	2.0809 -2.3496	2.4529 -2.8292	2.7769 -3.2692	3.1578 -3.8103
400	2.0837 -2.3416	2.4568 -2.8234	2.7819 -3.2615	3.1643 -3.7999
420	2.0862 -2.3378	2.4638 -2.8131	2.7866 -3.2544	3.1764 -3.7983
440	2.0866 -2.3344	2.4638 -2.8131	2.7910 -3.2478	3.1761 -3.7814
46 <b>G</b>	2.0909 -2.3312	2.4669 -2.8084	2.7951 -3.2417	3.1815 -3.7731
49 <b>0</b>	2.0930 -2.3282	2.4699 -2.8041	2.7989 -3.2360	3.1865 -3.7655
500	2.0950 -2.3253	2.4727 -2.8001	2.8026 -3.2306	3.1913 -3.7583
520	2.1969 -2.3227	2.4754 -2.7963	2.8060 -3.2256	3.1957 -3.7515
540	2.1987 -2.3212	2.4779 -2.7927	2.8093 -3.2209	3.2000 -3.7452
560	2.1004 -2.3179	2.4803 -2.7894	2.8124 -3.2165	3.2040 -3.7392
580	2.1020 -2.3157	2.4826 -2.7862	2.8153 -3.2123	3.2079 -3.7336
6 <b>00</b>	2.1035 -2.3136	2.4847 -2.7832	2.9181 -3.2083	3.2115 -3.7283
6 <b>20</b>	2.1050 -2.3116	2.4868 -2.7813	2.8208 -3.2045	3.2150 -3.7232
640	2.1064 -2.3097	2.4887 -2.7776	2.8233 -3.2010	3.2183 -3.7184
660	2.1077 -2.3079	2.4906 -2.7751	2.8257 -3.1976	3.2215 -3.7138
630	2.1090 -2.3062	2.4924 -2.7726	2.8281 -3.1943	3.2246 -3.7095
700	2.1102 -2.3045	2.4942 -2.7713	2.8303 -3.1912	3.2275 -3.7053
720	2.1114 -2.3030	2.4958 -2.7680	2.8325 -3.1883	3.2303 -3.7014
740	2.1125 -2.3015	2.4974 -2.7659	2.8345 -3.1854	3.2330 -3.6976
760	2.1136 -2.3000	2.4989 -2.7638	2.8365 -3.1827	3.2356 -3.6940
780	2.1147 -2.2987	2.5304 -2.7618	2.8384 -3.1811	3.2381 -3.6905
8 <b>00</b>	2.1157 -2.2973	2.5018 -2.7599	2.8443 -3.1776	3.2405 -3.6871
820	2.1166 -2.2961	2.5032 -2.7581	2.8421 -3.1752	3.2429 -3.6839
840	2.1176 -2.2948	2.5046 -2.7564	2.8438 -3.1729	3.2451 -3.6808
860	2.1185 -2.2937	2.5058 -2.7547	2.8455 -3.1737	3.2473 -3.6778
880	2.1194 -2.2925	2.5071 -2.7531	2.8471 -3.1686	3.2494 -3.6750
9 <b>00</b>	2.1202 -2.2914	2.5083 -2.7515	2.8486 -3.1665	3.2514 -3.6722
920	2.1210 -2.2904	2.5094 -2.7500	2. 8501 - 3.1645	3.2534 -3.6695
	2.1218 -2.2893	2.5106 -2.7485	2. 8516 - 3.1626	3.2553 -3.6669

## APPENDIX B

This appendix presents the computer program used to compute the density functions for a specified extreme mean and its confidence intervals.

```
PROGRAM MAIN (OUTPUT, TAPE 13)
      COMMON /SHARE/ N(41), K, DEN(103,9), DIST(103,9), T(103), INDEX(9)
       COMMON /CHARE/ A(41), B(41), C(41), D(41), DD(41), F(41)
                    ROUTINE TO PRODUCE TABLE FOR DISTRIBUTION OF
C4+++
                    VALUES ABOVE A..
C****
C***
                    CONFIDENCE INTERVAL COMPUTATIONS ..
C****
      DATA N/30,40,50,60/
      AA = 1.753975
      00 1 I=5,39
      N(I) = 60 + I - 4
C***
      N(48) = 180
      N(41) = 120
C****
      DO 7 L=1,2
      DO 2 J=1,3
      00 4 I=1,41
      IF(N(I).LF.120)
     -F(I)=SORT(FLOAT(N(I)-1)/2.)+GAMMA(FLOAT(N(I)-1)/2.)/GAMMA(FLOAT(N(
     -I))/2.)
      IF (N(I).GT.12C)
     -F(I) =EXP(+.5)*(FLOAT(N(I)-1)/FLOAT(N(I)))**((FLOAT(N(I))-1.)/2.)
      A(I) = . 1./SQRT(FLOAT(N(I))) + AA*F(I)/SQRT(FLOAT(2*N(I)-1))
      B(I) = AA*(F(I)*SQRT(FLOAT(2*N(I)-3)/FLOAT(2*N(I)-2))-1.)
      OD(I) = FLOAT(N(I))*AA*AA*(F(I)*F(I)-1.)
      C(I) = SQFT((1.+00(I)))/FLOAT(2*N(I)*N(I)-1))
    4 O(I) = SORT(FLOAT(2*N(I)-3))
      IF(L.EG.2)3,6
                    FRINT RESULTS, TABLE 1..
    6 IF(J.EQ.1) CALL PRINT1
C****
                    FRINT RESULTS, TABLE 2..
    3 IF (J.EQ.2) CALL PRINT2
      IF (J.E0.3) PRINT 104
       FORMAT (" "76 ("-"))
  104
      CONTINUE
  2
C****
      CALL DRAW1
      N(1) = 148
      DO 98 K=2.41
   98 N(K)=N(K-1)+26
C***
    7 K=0
C****
      CALL PLOT (0.,0.,999)
      END
```

```
SUBROUTINE DRAW1
      DIMENSION ZNORM (183,9)
      COMMON /SHARE/ N(41), K, DEN(103,9), DIST(103,9), T(103), INDEX(9)
      COMMON /CHARE/ A(41), B(41), C(41), D(41), DD(41), F(41)
      DATA INDEX/1,2,3,4,14,24,34,40,41/
      DATA FI/172162207732584285518/
      CALL PLOTS (0,0,13)
      CALL FACTOR(2./2.54)
      CALL PLOT (1.,2.,-3)
      T(102) = -5.
      T(103) = 1.
      ZNORM(1)2) = 0.
      ZNGRM(103) = .05
C****
                    FILL ARRAYS WITH DENSITY AND DISTRIBUTION VALUES...
C****
      DO 109 K=1,9
      I = INDEX(K)
C****
      DO 3 J=1,161
      T(J) = -5. + FLOAT(J-1)/10.
      ZNORM(J) = 1./SORT(2.*PI*EXP(T(J)*T(J)))
      X = (C(I)*i(I)*I(J) - B(I))/(A(I)*C(I)*T(J))
      DIST(J,K) = FNORMAL(X)
      DEN(J,K) = C(I)*(A(I)*D(I)-B(I))/(SQRT(2.*FI)*(A(I)-C(I)*T(J))**2)
     -+EXP(-(C(I)+D(I)+T(J)-9(I))++2/(2.*(A(I)-C(I)+T(J))++2))
  3
      CONTINUE
C****
      CALL AXIS(0.,u.," ".-1,13.,0.,-5.,1.)
      CALL AX93 (5.,0.," ",1,8.,90.,0.,05)
      DEN(102,K) = 0.
      DEN(103.K) = .05
C****
                    DO THE PLCTTING STUFF ....
      CALL LINE (T, DEN(1, K), 161, 1, 0, 0)
      CALL DASHL (T, ZNORM, 101,1,0,0)
      CALL SYMBOL(1.,8.5,.15,"DENSITY FUNCTION OF Z(...) AND T(-) = (MU H
     -HAT - MU)/S(MU HAT)", 0., 62)
      CALL SYMBOL (8.5,8.,.15,"N = ",0.,4)
      CALL NUMBER (9.1.8.,.15.FLOAT (N(INDEX(K))).0.,-1)
      CALL PLOT (12., 0., -3)
                    FRINT RESULTS, TABLE 3..
  109 CALL PRINT4
C****
      RETURN
      END
```

```
SUBROUTINE PRINT1
     DIMENSION Z(4)
     COMMON /SHARE/ N(41),K,DEN(103,9),DIST(103,9),T(103),INDEX(9)
     COMMON /CHARE/ A(41),8(41),C(41),D(41),DD(41),F(41)
     FCNU(A,3,C,0,Z) = (B+A+Z)/(C+(B+Z))
     FCNL(A+B+C+D+Z) = (B-A+Z)/(C+(D-Z))
     DATA Z/1.645,1.96, 2.24,2.576/
     PRINT 100, (N(I), F(I), SQRT((1.+DU(I))/FLOAT(N(I))), A(I), B(I), C(I),
  - -D(1).I=1.41)
166 FOFMAT(*1*,//,* TABLE 1.*,/,T10,"VARIOUS FUNCTION OF N NEEDED IN
    -THE CALCULATION OF THE", /, T10, "DISTRIBUTION OF T = (MU HAT - MU)/S
    - (MU HAT) ", //, T15, "F = (GAMMA((N-1)/2)/GAMMA(N/2)) *SQRT((N-1)/2)", /
                    115,"01 = N*(F*F - 1)*A1*A1",/,
    -,
                    115,"A = 1./SQRT(N) + A1*F*(1./SQRT(2*(N-1)))",/,
                    T15,"B = A1*(F*SQRT(2*N-3)/(2*N-2)) -1)",/,
                    T15,"C = SQRT( (1 + D1)/(2*N*(N-1) )",/,
                   T15,"D = SORT(2*N-3)",///,
        N",T13,"F",T20,"SQRT((1+D1)/N)",T38,"A",T48,"8",T58,"C",T68,"D"
    -(" "I3,T9,F9.6,T20,F9.6,T33,F9.6,T43,F9.6,T53,F9.6,T63,F9.6))
     RETURN
     ENTRY FRINTS
   4 PRINT 132, (N(I), (FLNU(A(I), B(I), C(I), D(I), Z(M)),
                   FCNL(A(I),B(I),C(I),D(I),Z(M)),M=1,4),I=1,41)
 102 FORMAT ("1",//" TABLE 2: UPPER AND LOWER CONFIDENCE BOUNDS OF T =
    -(MU HAT - MU)/5(MU)"/T15,"FOR ALPHA =0.90, 0.95, 0.975, AND 0.99"//
    - T12,"(=.9"
    -/T12, "UPPER BOUND = (8+A+Z)/(C+(0+Z)), LOWER BOUND = (8-A+Z)/(C+(D+Z))
    --Z)) "/,T15,"(Z VALUES ARE STANDARD NORMAL VALUES FOR ALPHA) "//" ",
    -76("-"),/,T2,"SAMPLE",19,"I ALPHA = 0.90",T26,"I ALPHA = 0.95",T43
    -,"I ALFHA = 0.975", T60, "I ALPHA = 0.99", T77, "I", /, T9,69("-"), /, -T4, "SIZE", T9, "I UPPER I LOWER", T26, "I UPPER I LOWER", T43, "I UPPE
    -R I LCWER", TED, "I UPPER I LOWER", T77, "I", /, T9,
-"I BOUND I BOUND", T26, "I BOUND I BOUND", T43, "I BOUND I BOUND",
    -T6(,"I BOUND I BOUND",T77,"I",/,T2,76("-"),/
            (" "13, T9, "I ", F6. 4, 1X, F7. 4, T26, "I ", F6. 4, 1X, F7. 4, T43, "I ",
    -F6.4.1X.F7.4.T60,"I ".F6.4.1X.F7.4.T77,"I"))
     RETURN
     ENTRY PRINT4
     PRINT 136, N(INDEX(K)),(T(II),DEN(II,K),DIST(II,K),T(II+50),DEN(II
    -+50,K),OIST(II+50,K),II=1,50)
 106 FORMAT (*1*,//," TABLE 3. DENSITY ( D(T) ) AND DISTRIBUTION ( F(T
    -) ) OF THE RANDOM VARIABLE"/, T15, "T = (MU HAT - MU)/S(MU HAT)
    -N = ... 13.//.
    -112, "T", T22, "C(T)", T32, "F(T)", T45, "T", T55, "C(T)", T65, "F(T)",/,
    -( 10(* *,110,F6.2,T20,F9.6,T30,F9.6,T43,F6.2,T53,F9.6,T63,F9.6,/)
    -))
     RETURN
     END
```

```
SUBROUTINE CINTRVL(XBAR, SIGMA, FCNU, FCNL, N, XLOW, XHIGH)
C****
C***
                     SUBROUTINE TO PRODUCE 95 PERCENT CONFIDENCE INTERVALS
C***
                     FOR EXTREEM MEAN
C + + +.*
C++++
                     BY BROWNLOW, SDC/ISI 3/79
C****
                     INFUT :
C + + + +
                       XBAR GATA MEAN
                       SIGMA DATA STANDARD DEVIATION
                       FCNU.FCNL FUNCTIONAL VALUES PASSED IN FROM
                       N NUMBER OF OBSERVATIONS IN THE SAMPLE... MAIN ROUTINE WRITTEN BY CRUM.
                    CUTPUT:
                       XLOW LOWER CONFIDENCE INTERVAL VALUE
                       XHIGH UPPER CONFIDENCE INTERVAL VALUE.
C***
C * * * *
C++++
                    FOR VARIOUS PROBABILITY VALUES, AA AND Z MUST
C***
                    RE CHANGED. .
C++++
                      SEE PAPER FOR DETAILS...
C***
      AA = 2.362712834
      7 = 1.644853628
C****
C++++
      FN = N
      F = EXF(.5)*((FN-1.)/FN)**((FN-1.)/2.)
C****
      DD = FN*AA*(F*F-1.)
      XLCH = XBAR + AA*F*SIGMA - FCNU*SIGMA*SQRT((1.+DD)/FN).
      XHIGH = XBAR + AA*F*SIGMA - FCNL*SIGMA*SORT((1.+DD)/FN)
C++++
C****
C****
      RETURN.
      ENU
```

### **REFERENCES**

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